Reinforcement Learning with Human Feedback

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Presentation

Part 1	Typical RL setting
	Case for preference-based learning
	Choice Models, BTL
	(Deep) Learning from human preferences and PbRL paper
Part 2	RLHF pipeline
	Primer for the PPO algorithm
	PPO algorithm
	DPO algorithm
Part 3	Limitations

Part 4

Conclusion and after thoughts

Part 1

- A typical RL setting
- Making a case for preference-based learning.
- Choice Models: BTL
- (Deep) Learning from human preferences and PbRL paper

Success of Reinforcement Learning



Game playing, robotics, online shopping





Inventory management, Resource management/Queuing







- 1. Large but tractable set of state and actions
- 2. Markovian transitions.



- (Largely) offline problem
- Past data = $\{s_1, a_1, s_2, a_2, \dots s_T, a_T\}$.
- Potential goals
 - (Task learning) reach a goal state fast
 - (Long-term decision making) prioritize reaching certain "good" states often.
- Train a loss function that emphasizes the desired goal(s) and finds a good policy.



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- Past data = { $s_1, a_1, r_1, s_2, a_2, r_2 \dots s_T, a_T, r_T$ }.
- Potential goals
 - (Task learning) reach a goal state fast : high reward for the goal state, negative reward for non-goal states.
 - (Long-term decision making) prioritize reaching certain "good" states often: choice of reward selection.
- Train a loss function that emphasizes the desired goal(s) and finds a good policy.

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1. Large but tractable set of state and actions

- Past data = { $s_1, a_1, r_1, s_2, a_2, r_2 \dots s_T, a_T, r_T$ }.
- Define Value function $V^{\pi} = E_{a \sim \pi, s \sim P}[\sum_{t \geq 1} \gamma^{t} r(s_{t}, a_{t})], 0 < \gamma \leq 1.$

• Find
$$\pi$$
 such that $V^{\pi^*} - V^{\pi} \leq \epsilon$, $V^{\pi^*} = \max_{\pi'} V^{\pi'}$.



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- Reward feedback can be provided by human labelers, machine etc.
- Primary difference that we consider is that there is trajectory level preference feedback.

Typical RL instance requires significant reward-engineering, domain knowledge and definition of a compact reward function.

• Reward hacking

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 - Example: robot picking a glass what is a good reward function? Goal "image" of glass in air? What if the glass has a dark liquid or background changes?

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• Multi-objective reward

• Example: Economic policies that prioritize economic growth without letting inflation grow too much.

Preference-based learning

- $\tau_1 = \{s_1, a_1, s_2, a_2, \dots, s_t, a_t\}$ and $\tau_2 = \{s'_1, a'_1, s'_2, a'_2, \dots, s'_t, a'_t\}$. Typical feedback $\{\tau_1 \ge \tau_2\}$.
- Can utilize expert feedback, non-expert "common-sense" feedback
- Comparing two options is often easier than generating an expert trajectory (Imitation learning) or finding a reward function first from human demonstrations (Inverse RL) to train an agent.

Preference modeling example

- There are 30 basketball teams in the NBA, each playing 82 games in the regular season (so there are 1230 total games).
- We observe, at the end of the regular season, which two teams (*i*, *j*) played in each game, and whether team i or team j won.
- How can we rank the teams and/or determine the strength of each team?

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- How can we rank the teams and/or determine the strength of each team?
- The simplest strategy might be to compare the number of games won by each team.
- However, the NBA season is structured so that every team plays every other team a different number of times (between 2 and 4).
- The teams have different "strengths of schedule", meaning that some teams play stronger opponents more frequently than do other teams.
- These teams might have worse win-loss records, but in fact be better than other teams that won more games against weaker opponents.

Bradley-Terry Model (BTL)

- Let $\beta_i \in R$, denote the strength of team *i*.
- Let the outcome of the game between teams *i*, *j* be determined by $\beta_i \beta_j$.
- Then **Bradley Terry Model** assumes the outcome as an independent Bernoulli random variable with distribution Bernoulli (p_{ij}) , where the log-odds corresponding to the probability p_{ij} that the team i beats team j is modeled as,

$$\log\left(\frac{p_{ij}}{1-p_{ij}}\right) = \beta_i - \beta_j.$$
$$p_{ij} = \frac{e^{\beta_i - \beta_j}}{1 + e^{\beta_i - \beta_j}} = \frac{e^{\beta_i}}{e^{\beta_i} + e^{\beta_j}}.$$

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- Invariant under constant scaling, outcomes independent of non-competing teams
- Model can be enhanced by parametrizations and link functions $\beta_i \leftarrow \sigma(f(\beta_i))$.







labels:

$$\operatorname{loss}(\hat{r}) = -\sum_{(\sigma^1, \sigma^2, \mu) \in \mathcal{D}} \mu(1) \log \hat{P} \big[\sigma^1 \succ \sigma^2 \big] + \mu(2) \log \hat{P} \big[\sigma^2 \succ \sigma^1 \big].$$

"Deep Reinforcement Learning from Human Preferences", 2017



Part 2

- PPO algorithm
- RLHF
- DPO algorithm

A primer to the (Proximal Policy Optimization) PPO algorithm: Non-RL view

Minorize-Maximization (MM) Algorithm

How to optimize a function like $f(\theta) = V^{\pi_{\theta}}$?

Steps in MM algorithm



Minorize-Maximization (MM) Algorithm

How to optimize a function like $\eta(\theta) = V^{\pi_{\theta}}$?

Steps in MM algorithm

- The algorithm proceeds in iteration i = 1,2,3, ...
- Let $M_i = g(\theta | \theta_i)$ be a surrogate which be **minorized version** of the objective function $f(\theta)$, satisfying
 - $g(\theta|\theta_i) \leq f(\theta) \forall \theta$.
 - $g(\theta_i|\theta_i) = f(\theta_i).$
- The algorithm maximizes $g(\theta|\theta_i)$ instead:
 - $\theta_{i+1} = argmax_{\theta}g(\theta|\theta_i).$

The above method guarantees that $f(\theta_i)$ converges to a local optima or saddle point as $i \to \infty$. $f(\theta_{i+1}) \ge g(\theta_{i+1}|\theta_i) \ge g(\theta_i|\theta_i) = f(\theta_i).$

- If $g(\theta) = f(\theta)$, that is if we optimize $V^{\pi_{\theta}}$ directly then we get the family of the policy gradient <u>algorithms.</u>
 - Examples include REINFORCE [Williams 1988, Williams 1992], DQN [2016], among others
 - Practical implementations still involved formulations (e.g. Baseline trick) and engineering heuristics (DQN for Atari)

policy gradient (steepest direction to maximize rewards)

$$A^{\pi}(s,a) = Q^{\pi}(s,a) - V^{\pi}(s)$$

$$T =
abla_ heta J(\pi_ heta) = \mathop{\mathrm{E}}_{ au \sim \pi_ heta} \left[\sum_{t=0}^\infty \gamma^t
abla_ heta \log \pi_ heta(a_t|s_t) A^{\pi_ heta}(s_t,a_t)
ight]^{-1}$$

$$\theta_{k+1} = \theta_k + \alpha g$$

take a gradient step in updating the policy

- If $g(\theta) = f(\theta)$, that is if we optimize $V^{\pi_{\theta}}$ directly then we get the family of the policy gradient <u>algorithms.</u>
 - Examples include REINFORCE [Williams 1988, Williams 1992], DQN [2016], among others
 - Practical implementations still involved formulations (e.g. Baseline trick) and engineering heuristics (DQN for Atari)





• First order methods assume the Value function surface to be flat. High curvature can be bad for learning

- If $g(\theta) = f(\theta)$, that is if we optimize $V^{\pi_{\theta}}$ directly then we get the family of the policy gradient <u>algorithms.</u>
 - Examples include
 - Practical implem (DQN for Atari)



• Susceptible to learning rate schedule, large policy changes

A primer to the PPO algorithm:

- Choice of $g(\theta)$ that minorizes $f(\theta)$
 - Key idea: We find π' that **locally** improves $J(\pi')$ when compared to $J(\pi_{old})$ for some π_{old} .
 - Suppose the objective is $\max_{\pi'} J(\pi') = E_{a \sim \pi', s \sim P}[\sum_{t \ge 1} \gamma^t r_t]$
 - We only care about the argmax policy
 - So instead consider the objective $f(\theta) = \max_{\pi'} J(\pi') J(\pi)$
 - We will find a function $g(\theta)$ that minorizes $f(\theta)$: [result of the famous TRPO 2015 paper]

$$J(\pi') - J(\pi) \geq \frac{\mathcal{L}_{\pi}(\pi') - C_{\sqrt{\sum_{s \sim d^{\pi}} [D_{\mathcal{KL}}(\pi'||\pi)[s]]}}{\mathsf{M}}$$

- Choice of $L_{\pi}(\pi')$ is very specific.
- Key point M is non-negative therefore we have monotonic improvement

A primer to the PPO algorithm

$$\max_{\pi'} \mathcal{L}_{\pi} (\pi') - C_{\sqrt{\sum_{s \sim d^{\pi_k}} [D_{\mathcal{K}\mathcal{L}}(\pi'||\pi)[s]]}}$$
or
$$\max_{\pi'} \mathcal{L}_{\pi} (\pi')$$
s.t. $\underset{s \sim d^{\pi}}{\to} [D_{\mathcal{K}\mathcal{L}}(\pi'||\pi)[s]] \leq \delta$

A primer to the PPO algorithm

$$\max_{\pi'} \mathcal{L}_{\pi} (\pi') - C_{\sqrt{\sum_{s \sim d^{\pi_k}} [D_{\mathcal{K}L}(\pi'||\pi)[s]]}}$$
or
$$\max_{\pi'} \mathcal{L}_{\pi} (\pi')$$
s.t. $\underset{s \sim d^{\pi}}{\to} [D_{\mathcal{K}L}(\pi'||\pi)[s]] \leq \delta$

- Approximate the expected advantage function locally around the current policy.
- The accuracy decreases when the new policy and the current policy diverge from each other.
- KL term acts as an upper bound for the error.

The PPO algorithm [2017]

• The two variants of the PPO algorithm

Algorithm 4 PPO with Adaptive KL Penalty

Input: initial policy parameters θ_0 , initial KL penalty β_0 , target KL-divergence δ for k = 0, 1, 2, ... do Collect set of partial trajectories \mathcal{D}_k on policy $\pi_k = \pi(\theta_k)$ Estimate advantages $\hat{A}_t^{\pi_k}$ using any advantage estimation algorithm Compute policy update

$$heta_{k+1} = rg\max_{ heta} \mathcal{L}_{ heta_k}(heta) - eta_k ar{D}_{ extsf{ extsf{KL}}}(heta|| heta_k)$$

by taking K steps of minibatch SGD (via Adam) if $\overline{D}_{KL}(\theta_{k+1}||\theta_k) \ge 1.5\delta$ then $\beta_{k+1} = 2\beta_k$ else if $\overline{D}_{KL}(\theta_{k+1}||\theta_k) \le \delta/1.5$ then $\beta_{k+1} = \beta_k/2$ end if end for

The PPO algorithm [2017]

• The two variants of the PPO algorithm

 $r_t(heta) = \pi_{ heta}(a_t|s_t)/\pi_{ heta_k}(a_t|s_t)$

Algorithm 5 PPO with Clipped Objective

Input: initial policy parameters θ_0 , clipping threshold ϵ for k = 0, 1, 2, ... do Collect set of partial trajectories \mathcal{D}_k on policy $\pi_k = \pi(\theta_k)$ Estimate advantages $\hat{A}_t^{\pi_k}$ using any advantage estimation algorithm Compute policy update

 $heta_{k+1} = rg\max_{ heta} \mathcal{L}^{\mathit{CLIP}}_{ heta_k}(heta)$

by taking K steps of minibatch SGD (via Adam), where

$$\mathcal{L}_{\theta_k}^{CLIP}(\theta) = \mathop{\mathrm{E}}_{\tau \sim \pi_k} \left[\sum_{t=0}^{T} \left[\min(r_t(\theta) \hat{A}_t^{\pi_k}, \operatorname{clip}\left(r_t(\theta), 1-\epsilon, 1+\epsilon\right) \hat{A}_t^{\pi_k}) \right] \right]$$

end for

The PPO algorithm [2017]

- The PPO algorithm is easy to implement in practice and works well.
- Only a few lines of code change from the vanilla policy gradient algorithm (clipped version works well)
- Paper shows it to perform better or similar than contemporary algorithms on variety of tasks.
- TRPO[2015] introduced the idea of using a surrogate loss to optimize the value function. PPO simplifies the implementation with stronger performance.

RLHF Pipeline and DPO

- <u>Key takeaway from PPO: we have a surrogate reward function that approximately</u> <u>minorizes the reward function of our interest, we optimize the surrogate reward function</u> <u>instead.</u>
- Foundation models may not have "human-need-aligned" output therefore they need to be fine-tuned to satisfy ethics/safety/security constraints or for a specific use-case.
- RLHF in the context of foundation model fine-tuning refers to a 3 step process, where PPO is used in the 3rd step.
- **Direct Preference Optimization (DPO)** is an efficient way of combining the 2nd and the 3rd steps of the RLHF pipeline.

Slides from Rafael Rafailov Archit Sharma Eric Mitchell

Direct Preference Optimization: A New RLHF Approach

Rafael Rafailov Archit Sharma Eric Mitchell





Stanford University
Step 1

Collect demonstration data, and train a supervised policy.

A prompt is \bigcirc sampled from our Explain the moon prompt dataset. landing to a 6 year old A labeler C demonstrates the desired output behavior. Some people went to the moon... This data is used to fine-tune GPT-3 with supervised learning.

l. BBB

Training language models to follow instructions with human feedback, Ouyang et. al. 2022 Stanford University



Step 2

Collect comparison data, and train a reward model.



Training language models to follow instructions with human feedback, Ouyang et. al. 2022 Stanford University



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Step 3

Optimize a policy against the reward model using reinforcement learning.

A new prompt is sampled from the dataset.

olicy

Write a story about frogs

The policy generates an output.

The reward model calculates a reward for

the output.

The reward is used to update the policy using PPO.



Training language models to follow instructions with human feedback, Ouyang et. al. 2022





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Preferred response

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Prompt Dispreferred response

Preferred response

Bradley-Terry Model connects rewards to preferences:

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Bradley-Terry Model connects rewards to preferences:

$$p(y_w \succ y_l \mid x) = \sigma(r(x, y_w) - r(x, y_l))$$

Feedback comes as preferences over model samples:

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Preferred response

Bradley-Terry Model connects rewards to preferences:

Reward assigned to preferred and dispreferred responses

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Preferred response

response

Bradley-Terry Model connects rewards to preferences:

 $p(y_w \succ y_l \mid x) = \sigma(r(x, y_w) - r(x, y_l))$

Train the reward model by **minimizing negative log likelihood:**

Feedback comes as preferences over model samples:

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Preferred response

Bradley-Terry Model connects rewards to preferences:

$$p(y_w \succ y_l \mid x) = \sigma(r(x, y_w) - r(x, y_l))$$

Train the reward model by **minimizing negative log likelihood:**

$$\mathcal{L}_R(\phi, \mathcal{D}) = -\mathbb{E}_{(x, y_w, y_l) \sim \mathcal{D}} \left[\log \sigma(r_\phi(x, y_w) - r_\phi(x, y_l)) \right]$$



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Sample from policy Want high reward...

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Now, learn a policy π_{θ} achieving **high reward** while **staying close** to original model π_{ref}

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Sample from policy Want high reward...

Now we have a **reward model** r_{ϕ} that represents* **goodness according to humans**

Now, learn a policy π_{θ} achieving high reward while staying close to original model π_{ref}

$$\max_{\pi_{\theta}} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi_{\theta}(y|x)} [r_{\phi}(x, y)] - \beta \mathbb{D}_{\mathrm{KL}} [\pi_{\theta}(y|x) || \pi_{\mathrm{ref}}(y|x)]$$
Sample from policy
Want high reward
but keep KL to original model smaller

...but keep KL to original model small!

Want high reward...

RLHF Objective

(get **high reward**, stay **close** to reference model)

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$$\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(y|x)} \left[r(x, y) \right] - \beta \mathbb{D}_{\mathrm{KL}} (\pi(\cdot \mid x) \| \pi_{\mathrm{ref}}(\cdot \mid x))$$

any reward function

 $\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(y|x)} \left[r(x, y) \right] - \beta \mathbb{D}_{\mathrm{KL}} \left(\pi(\cdot \mid x) \| \pi_{\mathrm{ref}}(\cdot \mid x) \right)$

RLHF Objective

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RLHF Objective

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Closed-form Optimal Policy

(write optimal policy as function of reward function; from prior work)

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Closed-form Optimal Policy

(write **optimal policy** as function of **reward function**; from prior work)

$$\pi^*(y \mid x) = \frac{1}{Z(x)} \pi_{\mathrm{ref}}(y \mid x) \exp\left(\frac{1}{\beta} r(x, y)\right)$$

RLHF Objective

$$\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(y|x)} \left[r(x, y) \right] - \beta \mathbb{D}_{\mathrm{KL}} (\pi(\cdot \mid x) \| \pi_{\mathrm{ref}}(\cdot \mid x))$$

and real free ations

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a maxima way and firm attack

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Note intractable sum over possible responses; can't immediately use this

RLHF Objective

$$\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(y|x)} \left[r(x, y) \right] - \beta \mathbb{D}_{\mathrm{KL}}(\pi(\cdot \mid x) \| \pi_{\mathrm{ref}}(\cdot \mid x))$$

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Rearrange

(write any reward function as function of optimal policy)

RLHF Objective (get high reward, stay close

to reference model)

 $\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(y|x)} \left[r(x, y) \right] - \beta \mathbb{D}_{\mathrm{KL}}(\pi(\cdot \mid x) \| \pi_{\mathrm{ref}}(\cdot \mid x))$

Closed-form Optimal Policy

(write **optimal policy** as function of **reward function**; from prior work)

$$\pi^{*}(y \mid x) = \frac{1}{Z(x)} \pi_{ref}(y \mid x) \exp\left(\frac{1}{\beta}r(x, y)\right)$$
with $Z(x) = \sum_{y} \pi_{ref}(y \mid x) \exp\left(\frac{1}{\beta}r(x, y)\right)$
Note intractable sum over possible responses; can't immediately use this

Rearrange

(write any reward function as function of optimal policy)

$$r(x,y) = \beta \log \frac{\pi^*(y \mid x)}{\pi_{ref}(y \mid x)} + \beta \log Z(x)$$

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some parameterization of a reward function

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RLHF Objective

any reward function $\max_{\pi} \mathbb{E}_{x \sim \mathcal{D}, y \sim \pi(y|x)} \left[r(x, y) \right] - \beta \mathbb{D}_{\mathrm{KL}}(\pi(\cdot \mid x) \| \pi_{\mathrm{ref}}(\cdot \mid x))$

(get high reward, stay close to reference model)

Closed-form Optimal Policy

(write optimal policy as function of reward function; from prior work)

$$\pi^{*}(y \mid x) = \frac{1}{Z(x)} \pi_{\mathrm{ref}}(y \mid x) \exp\left(\frac{1}{\beta}r(x, y)\right)$$
with $Z(x) = \sum_{y} \pi_{\mathrm{ref}}(y \mid x) \exp\left(\frac{1}{\beta}r(x, y)\right)$
 \longrightarrow Note intractable sum over possible responses; can't immediately use this

Ratio is **positive** if policy likes response more than reference model, negative if policy likes response less than ref. model

`

Rearrange

(write anv reward function as function of optimal policy)

 $r(x,y) = \beta \log \frac{\pi^*(y \mid x)}{\pi_{rof}(y \mid x)} + \beta \log Z$

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some parameterization of a reward function

A loss function on reward functions

A loss function on reward functions

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A transformation between <u>reward</u> <u>functions</u> and <u>policies</u>

A loss function on reward functions

A transformation

between <u>reward</u> <u>functions</u> and <u>policies</u>

A loss function on policies
Derived from the Bradley-Terry model of human preferences:

$$\mathcal{L}_R(r, \mathcal{D}) = -\mathbb{E}_{(x, y_w, y_l) \sim \mathcal{D}} \left[\log \sigma(r(x, y_w) - r(x, y_l)) \right]$$

A loss function on <u>reward functions</u>



A transformation between <u>reward</u> <u>functions</u> and <u>policies</u>

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A loss function on reward functions



A transformation between <u>reward</u> <u>functions</u> and <u>policies</u>

$$r_{\pi_{\theta}}(x, y) = \beta \log \frac{\pi_{\theta}(y \mid x)}{\pi_{\mathrm{ref}}(y \mid x)} + \beta \log Z(x)$$

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A transformation between <u>reward</u> <u>functions</u> and <u>policies</u>

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policies

$$r_{\pi_{\theta}}(x,y) = \beta \log \frac{\pi_{\theta}(y \mid x)}{\pi_{ref}(y \mid x)} + \beta \log Z(x)$$
Reward of
preferred
response

$$\mathcal{L}_{\text{DPO}}(\pi_{\theta}; \pi_{ref}) = -\mathbb{E}_{(x,y_w,y_l)\sim\mathcal{D}} \left[\log \sigma \left(\beta \log \frac{\pi_{\theta}(y_w \mid x)}{\pi_{ref}(y_w \mid x)} - \beta \log \frac{\pi_{\theta}(y_l \mid x)}{\pi_{ref}(y_l \mid x)} \right) \right]$$

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A loss function

on <u>policies</u>

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A loss function on reward functions



A transformation between <u>reward</u> <u>functions</u> and <u>policies</u>

$$r_{\pi_{\theta}}(x, y) = \beta \log \frac{\pi_{\theta}(y \mid x)}{\pi_{\text{ref}}(y \mid x)} + \beta \log Z(x)$$

When substituting, the log Z term cancels, because the loss only cares about difference in rewards

A loss function
on policies
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A loss function on reward functions



A transformation between <u>reward</u> <u>functions</u> and <u>policies</u>

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Reward of **preferred** response

Reward of dispreferred response

RLHF Pipeline and DPO

- <u>Key takeaway</u>: Direct Preference Optimization (DPO) fits an implicit reward function and optimizes for a good policy.
- DPO has a better performance than PPO (PPO + explicit reward function fitting)
- DPO is more robust to reward hacking as compared to PPO (PPO + explicit reward function fitting)

Part 3

• Limitations

• Practical aspects: the optimal design problem and credit assignment

- BTL model
 - Does not allow non-transitive preferences

Some may like apples over bananas, oranges over apples but bananas over oranges.

• Even if individuals have transitive preferences, then the expected preferences may not be transitive.

How to aggregate preferences over a population but still personalize.

- BTL model
 - Does not allow non-transitive preferences
 - Even if individuals have transitive preferences, then the expected preferences may not be transitive.
- RLHF pipeline/DPO pipeline
 - Success depends heavily on the choice of π_{ref}

This was the policy of the already fine tuned foundation model.

• Hard to quantify how good is the optimized policy wrt π_{ref}

How useful is the RLHF/DPO pipeline?

- BTL model
 - Does not allow non-transitive preferences
 - Even if individuals have transitive preferences, then the expected preferences may not be transitive.
- RLHF pipeline/DPO pipeline
 - Success depends heavily on the choice of π_{ref}
 - Hard to quantify how good is the optimized policy wrt π_{ref}
- About Data acquisition
 - Which contexts/prompts need fine tuning and what token sequences to offer to humans to label?
 - The human labeling is costly and slow.

The issue of Hindsight Credit assignment: Broader limitation with preference modeling.

Slides from "https://runzhe-yang.science/princeton-cs/demo/hindsight_credit_assignment.pdf"

Value Function Problem

$$V^{\pi}(x) \stackrel{\text{def}}{=} \mathbb{E}_{\tau \sim \mathcal{T}(x,\pi)} \Big[Z(\tau) \Big], \qquad Q^{\pi}(x,a) \stackrel{\text{def}}{=} \mathbb{E}_{\tau \sim \mathcal{T}(x,a,\pi)} \Big[Z(\tau) \Big].$$

"how does the current action affect future outcomes?"



Credit Assignment Problem

$$I(A_t; f(\tau_{t:\infty})|X_t = x) = \mathbb{E}_{\tau \sim \mathcal{T}(x,\pi)} \left[\log \left(\frac{\mathbb{P}(A = A_t | f(\tau) = f(\tau_{t:\infty}), X_t = x)}{\mathbb{P}(A = A_t | X_t = x)} \right) \right]$$

"given an **outcome**, how *relevant* were **past decisions**?"



Credit Assignment Problem - Why is it important?



Rare events require an infeasible number of samples to obtain an accurate estimate.



Issue 1: Variance - low sample efficiency



Issue 2: Partial observability - cannot bootstrap.



Issue 3: Time as a proxy - rely on *time* as the sole metric.



Issue 4: No counterfactuals - only update actions serendipitously occur.

Part 4

• Conclusion and after thoughts

Conclusion and After-thoughts

Summary

- Preference feedback is powerful way of awarding rewards in RL.
- PPO is a good, policy gradient style algorithm.
- RLHF in the context of LLMS refer to a pipeline of three step procedure useful in fine-tuning the foundation model for a specific task
- DPO is an efficient way of combining the steps 2 and 3 of RLHF for LLM.